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## Estimation of electrical formation factor and porosity from VES for the aquifers in parts of Bayelsa state Nigeria

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### Abstract

An attempt has been made to estimate the formation factor and porosity of the Quaternary Alluvial aquifers in parts of Bayelsa State, in Southern Nigeria. Formation factor ( $F$ ) is a very prominent parameter in most Geophysical investigations; it is fundamentally an indispensable factor in the evaluation of the petrophysical characteristics of repositories. The electrical formation factor (or formation resistivity factor),  $F_a$ , was evaluated from modelled resistivity data. In this study, the formation factor was estimated following Archie's original formulation and the corrected formation factor  $F_c$ , was estimated following the Waxman-Smits model. Formation factor obtained ranges from 1.41-47.5 with an average of 12.49. The spatial distribution of formation factor in the study area as here presented, shows that formation factor is of highest values in the west central parts and lower in the central parts of the Study area. We attribute the relatively low Formation factor values, in some areas to low pore water resistivity, which ranges from 6 - 179  $\Omega\text{m}$ , with an average of 69.2  $\Omega\text{m}$ ; as well as high bulk resistivity values ranging from 82 - 1894  $\Omega\text{m}$ , with an average of 441  $\Omega\text{m}$ . The estimated porosity in the study area ranges from 12 to 57%, at VES stations of 7, 34 and 21. The spatial distribution of the estimated porosity is shown in Fig. 8. The Porosity values obtained from the inversion of VES modelled parameters (Table 1) show that the porosity ( $\phi$ ) values range from 12% to 57%. The spatial distribution map of the estimated porosity is presented in Fig. 8, the Fig. shows that porosity values vary spatially from low values around the west central and south western parts to relatively high values around the north eastern parts of the study area. The calculated porosity values of an aquifer using average resistivity values are considered average porosity values, this is worthy of note because the resistivity values obtained from VES analysis are themselves average values, constructed from all of the smaller scaled heterogeneities within each layer.

**Keywords:** Repositories, formation factor, alluvial, porosity

### 1. Introduction

A very prominent parameter in Geoelectric investigation is the formation factor ( $F$ ); it is fundamentally an indispensable factor in the evaluation of the petro physical characteristics of repositories, engineering construction sites, as well as groundwater aquifers.

Understanding the formation factor is essential in using electrical and electromagnetic methods to monitor leachate accumulations and movements both within and around landfills. Specifically, the formation factor allows leachate resistivity, the degree of saturation, and, possibly, even the hydraulic conductivity of the waste to be estimated from non-invasive surface measurements. The concept of formation factor was first introduced by Sundberg (1932) <sup>[18]</sup>, who examined the ratio of rock resistivity to that of a conductive pore fluid.

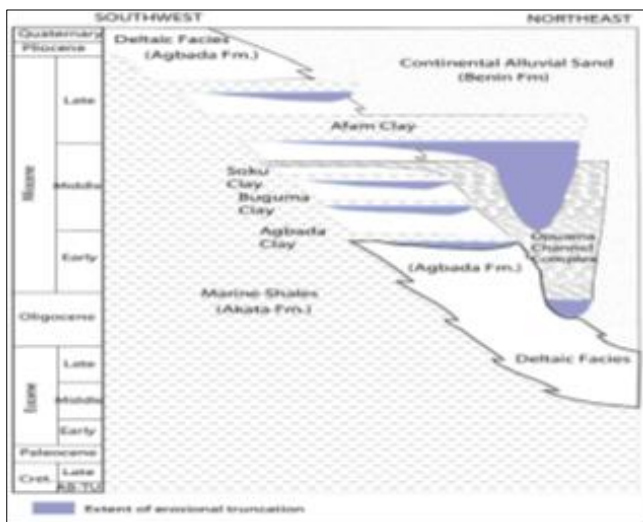
The ratio of a rock's resistivity when brine fully saturates it to the brine's resistivity is the formation resistivity factor as originally

designated by Archie (1942) [2]. By this definition,  $F$ , is independent of the resistivity of the Brine that saturates the rock (Wyllie and Rose, 1950) [14]. This definition of  $F$ , implicitly has the supposition, that, the solid matrix of the formation is a non-conducting (insulator) material. However, if the solid matrix is a conductive, the independence of  $F$ , on the resistivity of the fluid that saturates it will no longer exist, in such cases a correction factor may be included to accommodate for the conductive solids present in the rock matrix and if this correction is made, it is theoretically possible to determine,  $F$ .

The formation resistivity factor is usually determined by various physical parameters and lithological features, including electrical resistivity, pore water resistivity, temperature, viscosity, and extent of pore water saturation etc (Salem 1994; Salem, 2001) [15, 16].

### 1.1 The study area

Bayelsa State is one of six states (Edo, Bayelsa, Delta, Rivers, Cross Rivers, and Akwa Ibom) that make up the South-South geopolitical zone of Nigeria.



**Fig 1:** Stratigraphic sequence of the Niger Delta with the three Formations

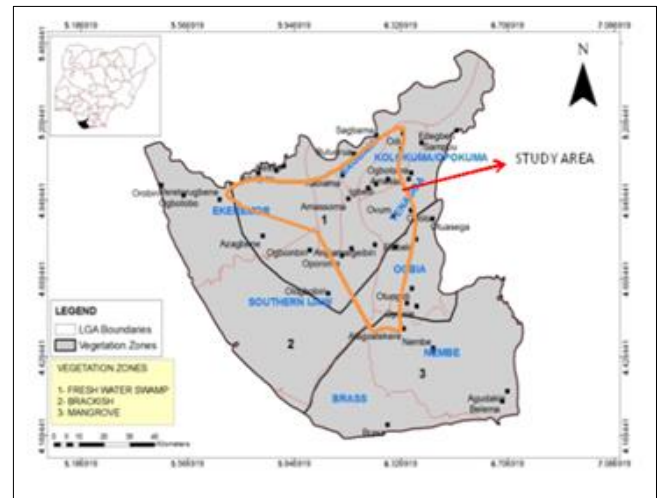
The name Bayelsa comes from the three previous major local government areas, Yenagoa (Yelga), Brass (Balga), and Sagbama (Salga) (Fig.1). The geographical position of Bayelsa State lies at  $4^{\circ} 15'$  north latitude and  $5^{\circ} 23'$  south latitude and  $5^{\circ} 22'$  west longitude and  $06^{\circ} 45'$  east. The state of Bayelsa is a picturesque rainforest having an approximate area of 21,110 Kilometer squared.

Over three quarter of the State is Riverine, characterized by a moderately low-lying land, stretching from Nembe to Ekeremor. The area is almost below sea level, with a labyrinth of winding streams and mangroves. Major rivers in the state are, Ramos, Nun, St. Nicholas, Sangana, Fishtown, Ikebiri Creek; others are, St. Barthelemy, Brass, Pennington, Dobo Middleton and Digatoro Creek; all of which flow into

the Atlantic Ocean by a network. of various streams and Rivers (BIPA, 2018) [3].

### 1.2 Stratigraphy of the Niger Delta region of Nigeria

Bayelsa State is part of the Niger Delta sedimentary Basin, which is located between latitudes  $3^{\circ} - 6^{\circ}N$  and longitude  $5^{\circ} - 8^{\circ}E$  (Fig.1). The Niger Delta basin Stratigraphically is categorized into three formations known as, Benin, Agbada and Akata, Formations, in order of increasing age (Fig.2). From apex to coast the sub-aerial portion stretches more than 300km, covering an area of 75,000 km<sup>2</sup>. The Niger Delta is an active sedimentary basin at present and has prograded since Details of the subsurface of the Niger Delta has fully revealed these three lithostratigraphic units, in the order of the youngest to the oldest, beginning from the Benin to the Agbada and then to the Akata, formation (Short & Stauble, 1967, Uko *et al.* 2002) [7, 20].



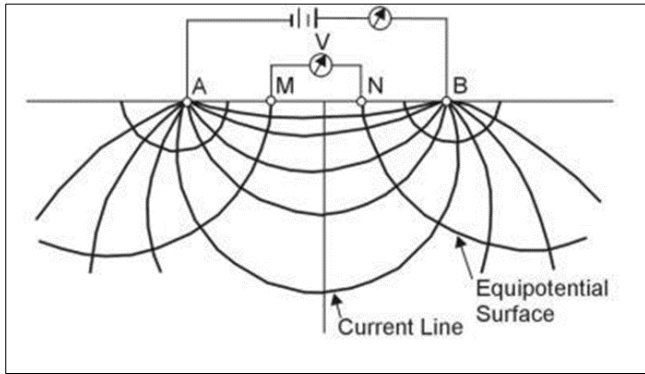
**Fig 2:** Bayelsa State map with the study area shown (Inset: Bayelsa in map of Nigeria)

### 2. Background Theory

Electrical resistivity techniques have been well-established and ubiquitously employed in resolving various geotechnical, geological, geophysical, environmental and groundwater problems (Amakiri *et al.* 2023 and Ward, 1990) [1, 23]. The primary purpose of the resistivity method is to measure the electric potential on the earth surface as a result of current flow within the earth.

Electric potential distribution in a soil in the vicinity of an electrode carrying current depends on the electric resistivity and the distribution of the surrounding rocks and soils. This basic understanding of physics is the basis for surface electrical resistivity surveying. A schematic of the equipotential surfaces and current lines that results are shown in Figure 2.1. Electric current flow through the ground is a function of several factors, which also depends on the location and the area's geology. The factors comprise of porosity, lithology, grain size, sediment depth, cementation, pore size and geometry, grading, compaction, packing,

groundwater, and groundwater salinity (Salem, 1999, Farid *et al.*, 2013) [15, 7].



**Fig 3:** Equipotential and current lines for a pair of current electrodes A and B, and a pair of Potential electrodes M and N, on a homogeneous half-space.

Several configurations for executing the Electrical resistivity survey exists, but the three most employed are shown in Figure 3, which are the Schlumberger, Wenner and the dipole-dipole arrays.

**2.1 Vertical Electrical Sounding**

The Vertical electrical sounding (VES) is a geoelectric method used for the investigation of the Earth’s subsurface, its basic principle helms from the fact that, when current is injected into the Earth by means of two (current) electrodes along a profile line, electric field is generated in the subsurface such that if two other (potential) electrodes are placed appropriately in line with the current electrodes, electric potentials difference can be measured between the two potential electrodes (Fig. 3). Depending on the configuration used, the apparent resistivity of the field investigation can be obtained as a function of the electrode spacing.

**2.1.1 The Schlumberger Array**

In the Schlumberger array (figure 4), two current electrodes (A and B) are separated a distance apart (AB) and two potential electrodes (M and N) are positioned in between the current electrodes such that the distance from each of the potential electrodes to each current electrode are equal and the center of the array is at the midpoint of M and N.

as  $\alpha$  (the potential electrodes interval) tends to zero, the term,  $V/\alpha$ , tends to the potential gradient value at the array centre. Practically the instrument’s sensitivity has a limitation on the ratio of,  $s$ , (the distance between the centre of the potential electrodes (the centre electrode) and one of the current electrodes to  $\alpha$ , and most often the range will be between 3 and 30. It is usually practicable, therefore, to use an electrode spacing that is finite with equation 2.15 to evaluate the geometric factor (Keller and Frischknecht, 1966) [12]. Consequently, the apparent resistivity ( $\rho_a$ ) can be given as:

$$\rho_a = \pi \left[ \frac{s^2}{\alpha} - \frac{\alpha}{4} \right] \frac{V}{I} = \pi \alpha \left[ \left( \frac{s}{\alpha} \right)^2 - \frac{1}{4} \right] \frac{V}{I} \tag{1}$$

Where,  $s$  is the distance between the midpoint of M and N and either of the current electrodes, A or B. The inner (potential) electrodes remain fixed in typical field operations, as the outside (current) electrodes are shifted with the distance,  $s$ . The spacing,  $\alpha$ , can only be altered when the sensitivity of the instrument’s measurement decreases. The spacing  $\alpha$  should not be greater than  $0.4s$  otherwise the assumption of a potential gradient will no longer be tenable. Again the,  $\alpha$  – spacing, can be varied, sometimes, without changing  $s$ , so that the detection of local in homogeneities or lateral variations present in the vicinity of the potential electrodes can be possible. For equal electrode spacing as in the Schlumberger configurations, the geometric factor,  $G$ , in Equ. 1 becomes,

$$G = \frac{\pi}{4} \left[ \frac{AB^2 - MN^2}{MN} \right] \tag{2}$$

Since in the Shlumberger configuration, the current electrode (AB) is usually much larger than the potential electrode (MN), Equ. (2) can be reduced to,

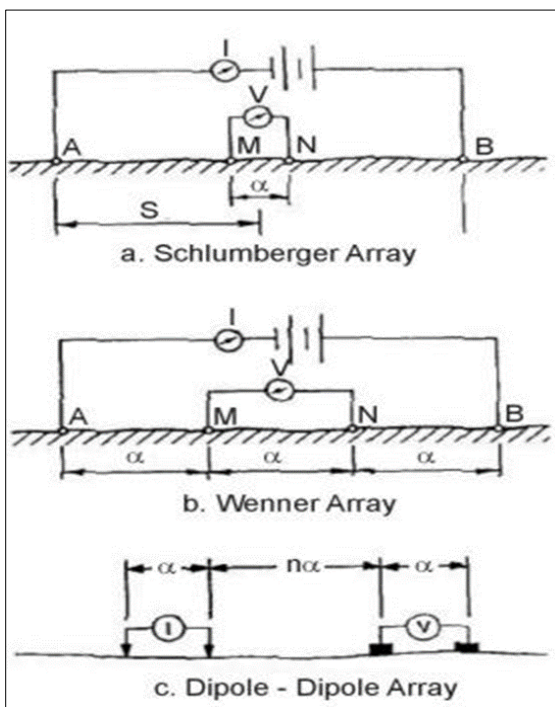
$$G = \frac{\pi}{MN} \left( \frac{AB}{2} \right)^2 \tag{3}$$

Equation (3) can also be expressed as;

$$G = \pi \frac{a^2}{b} \left[ 1 - \frac{b^2}{4a^2} \right] \tag{4}$$

Where,  $a = AB/2$  and  $b = MN$

When the formation geology is governed only by the vertical variation of the resistivity, a smooth curve will always result when the apparent resistivity is plotted against the configuration spacing. Inversions of resistance and irregularities in apparent resistivity curves, if not caused by errors, both point to lateral changes which would need to be further studied. When the Schlumberger arrangement is used, changing the potential electrode spacing may produce a displacement in the apparent resistivity curve due to lateral inhomogeneity. Such displacement can occur as a general displacement of the curve with no significant change of shape (Zohdy, 1968) [26].



**Fig 4:** Electrode configurations for resistivity measurements (a) Schlumberger (b) Wenner (c) Dipole-Dipole

### 3. Methodology

The methods used in obtaining the results presented in this study are here enumerated.

#### 3.1 Vertical Electrical Sounding (VES)

The vertical electrical sounding was executed in thirteen stations (VES1 to VES13) in the study, using the Schlumberger configuration.

##### 3.1.1 Vertical Electrical Sounding (VES)

The basic objective in carrying out a VES survey is to inverse the acquired field data so as to correspond to a subsurface geological or hydrogeological structure. To achieve this aim, it is important to adequately and satisfactorily interpret the acquired field data. The interpretation of VES field data can be implemented in two distinct ways, qualitatively or quantitatively. In the qualitative interpretation approach, the objective is to obtain the thickness and resistivity of the various geologic layers encountered. This is usually achieved analytically, empirically and semi empirically. While in the qualitative VES interpretation approach, the aim is to acquire information on the geological structure of the area under investigation. In this approach, 2D resistivity imaging and contour maps of different types are used to elucidate the detailed structures of the subsurface.

##### 3.1.2 Instrumentation

The equipment used in this study was a commercially available DC Terrameter SAS 1000 (Abem, Sweden). This equipment is a signal averaging system (SAS) resistivity measuring instrument, with reasonably high sensitivity. The Terrameter is rugged, user friendly and easy to carry about; it has been established that the equipment is very efficient, by reason of numerous uses in several investigation sites in Nigeria. The power source to the Abem Terrameter was a 12V battery and four stainless steel metal rods were used as the electrodes.

##### 3.1.3 Data Acquisition and Analysis

Twenty-one Vertical Electrical Soundings (VES) were executed with the DC resistivity meter (Abem Terrameter SAS 1000, (Fig. 3.2) making use of the Schlumberger configuration (Fig. 2.4). All the VES points were located in the vicinity of newly dug or preexisting boreholes, where geologic information was available. The Maximum current electrode half-spacing ( $AB/2$ ) used ranged between 30 and 250 m (i.e  $AB$  ranged from 60 – 500 m) with the assumption that depth penetration ranges between 0.25  $AB$  and 0.5  $AB$ . The centre point of the electrode array remained constant while the spacing of the electrodes was increased in order to obtain information from the successive greater depths. The current electrode separation ( $AB/2$ ) followed the sequence: 1.0, 1.5, 2.0, 2.5, 3.2, 4.0, 5.0, 6.0, 7.0, 8.0, 10.0, 12.0, 15.0, 20.0, 25.0, 30.0, 40.0, 50.0, 60.0, 70.0, 80.0, 100.0, 120.0, 150.0, 200.0, while the potential electrode spacing ( $MN/2$ ) was in the sequence: 0.3, 0.5, 1.0, 1.5, 2.5, 5.0, 7.5, 10.0, 15.0, and 25.0.

Data obtained using the Schlumberger configuration are mostly acquired in overlying segments since at each increasing level of the  $AB$  spacing, the signal output from the resistivity meter becomes weaker and weaker, consequently the potential electrode spacing ( $MN$ ) needed to be increased too and usually the  $AB/2$  values are measured twice, each for the short and long  $MN$  spacing. The Schlumberger

configuration was used not only because it is faster and most unlikely to be influenced by lateral variations, but also because it involves a minimum number of operators (because the current electrodes, A and B, are displaced away from themselves leaving the potentials electrodes, M unaffected). The resistance ( $R$ ) values obtained directly from the field survey served as the primary data which were used for the computation of the apparent resistivity ( $\rho_a$ ), by employing Equation 5. Von Nostrand and Cook (1984) has observed that, if  $MN$  is not more than two-fifth of  $AB$  ( $\frac{2}{5}AB$ ) then errors in apparent resistivity values will usually range from 2%-3%. The geometric factor ( $G$ ) used to obtain the apparent resistivity was obtained using Equation (3). The Apparent resistivity values were plotted against the half current electrode spacing ( $AB/2$ ) on a log-log scale. Guided by the general trend of the field curves, partial curve smoothening of the field curves were generated using the software IPI2win (2000) - a 1D resistivity interpretation software - and Interpex (1DXD). These plots constitute the field curves. The data obtained were later subjected to a computer assisted iterative interpretation using a 1D inversion technique software (1X1D, Interpex, USA) to obtain the one dimensional resistivity model for the area. This program utilizes the least-squares optimization technique, whereby the initial software model is successively adjusted until the difference between the observation and the output of the model is minimized. This program converts (or models) the field acquired apparent resistivities, as a function of the spacing of the electrode, to real resistivities, as a function of the depth. The field data is iteratively matched to a model curve calculated by the program. To build a model with the software, the interpreter subdivides the basement arbitrarily into several horizontal layers of different thicknesses. The resistivities are then iteratively modified by the program to obtain a better fit with the field data for the layer thicknesses chosen for the model. The resulting real resistivities represent the best average resistivity for the given layer.



**Fig 5:** Abem Terrameter and accessories (a. typical Abem Terrameter b. Typical accessories c. Abem Terrameter (SAS 1000) used in this study, d. Garmin etrex GPS used in the study).

### 3.2 Formation Resistivity factor

The electrical formation factor (or formation resistivity factor),  $F_a$ , was evaluated from the modelled field resistivity data following the expression given by Archie (1942) [2].

$$F_a = \frac{\rho_b}{\rho_w} = a\phi^{-m} \tag{5}$$

Where,  $a$ , is the pore geometry (or texture factor), usually ranging from 0.5 to 1.5;  $\rho_w$ , is the resistivity of the pore water;  $\rho_b$  is the aquifer bulk resistivity,  $\phi$ , is porosity (as a volume fraction) and  $m$ , in the original definition of Archie (1942) [2], is an exponent usually greater than 1.3. The term cementation factor for the exponent,  $m$ , was introduced by Guyod (1944) [9] since it may be qualitatively shown that formation factor tends to increase as the sand becomes more cemented, for any given porosity. Formation factor varies from unity (1) when the bulk resistivity equals the aquifer water resistivity, (at which instant the porosity is also unity) and increases as the porosity decreases. The formation factor is approximately constant for a given formation and is rarely less than unity, a situation that can only occur when the bulk resistivity is less than the aquifer water resistivity (Glover, 2015) [8]. To evaluate the formation factor, we used bulk resistivity ( $\rho_b$ ) values, obtained from the 1-D resistivity inversion while the measured pore water resistivity ( $\rho_w$ ) values, were obtained from bore holes in the vicinity of VES locations, which were taken to the laboratory, were the aquifer conductivity ( $\sigma$ ) was obtained and then converted to resistivity using the relation, Farid, *et al.*, (2013) [7]:

$$\rho = \frac{1000}{\sigma} \tag{6}$$

Available literature (e.g Waxman and Smits, 1968; Okiongbo and Soronnadi-Ononiwu, (2015) [22, 13] shows that this Archie’s relation is only valid for clean, clay-free sand sediments; hence the necessity for the compensation of the clay presence effect; which was achieved in this paper by introducing a correction factor to the formation factor. The study of the influence of clay content in geophysical parameters began with the work of Patnode and Wyllie (1950) [14], followed by Winsauer and McCardell (1953) [24], Hill and Milburn (1956) [10], and Waxman and Smits (1968) [22]. These works surmised that, when there are conductive materials between grains, the obtained factor is an *apparent* formation factor, in which case an analogy with electrical circuits can be adopted to calculate the formation factor of Clayey or Shaly formations (Diaz-Curiel *et al.* 2016) [5].

**3.2.1 Apparent formation factor,  $F_a$ , and corrected formation factor,  $F_c$**

In this study, the corrected formation factor  $F_c$ , was estimated following the Waxman-Smits (1968) [22] model, which is given as;

$$\frac{1}{F_a} = \frac{1}{F_c} + \left(\frac{BQ_y}{F_c}\right) \rho_w \tag{7}$$

In Equ.7, the coefficient  $BQ_y$ , is associated with the influences of surface conduction, basically resulting from the presence of clay particles, and when particles of clay are completely absent, the,  $F_a$  becomes equal to the corrected formation factor,  $F_c$ , (Supious, 2007; Okiongbo and Soronnadi-Ononiwu, 2015) [19, 13]. The inverse of the formation factor in Equation 3; is called the, ‘conductivity formation factor’ of the ‘connectedness of the rock, and it is the ratio of the fully saturated rock to that of the fluid/water (Glover, 2015) [8]. If  $1/F_a$  is plotted against pore fluid resistivity  $\rho_w$ , a straight line

graph is obtained in which the intercept of the straight line is represented by  $1/F_c$ , and the slope of the resulting curve is represented by the value of  $BQ_y/F_c$  (Devarajan *et al.*, 2006) [6]. Hence if  $1/F_a$  is plotted against the aquifer water resistivity ( $\rho_w$ ), a value for the corrected formation factor ( $1/F_c$ ) was obtained (Table 1).

**3.3 Porosity estimation from VES data**

Porosity of the aquifer was estimated from VES data by use of the modified Archie’s Equation, after Soupios (2007),

$$\phi = e^{\frac{1}{m} \ln(a) + \frac{1}{m} \ln\left(\frac{1}{F_c}\right)} \tag{8}$$

Where,  $\phi$ , is the porosity,  $m$  is the cementation factor and  $a$  is the pore geometry (coefficient of lithology), and  $F_c$  is the corrected formation factor. The values of the pore geometry,  $a$ , and the cementation factor,  $m$ , as obtained, from grain size porosities, were 0.65 and 1.98 respectively. The resulting porosities are shown in Table 1.

**4.0 Results and Discussion**

The results from the study are are presented as follows;

**4.1 Formation factor**

A plot of  $1/F_a$  against pore water resistivity ( $\rho_w$ ), is shown in Figure 6; where the established two trends of correlation are, Trend 1:

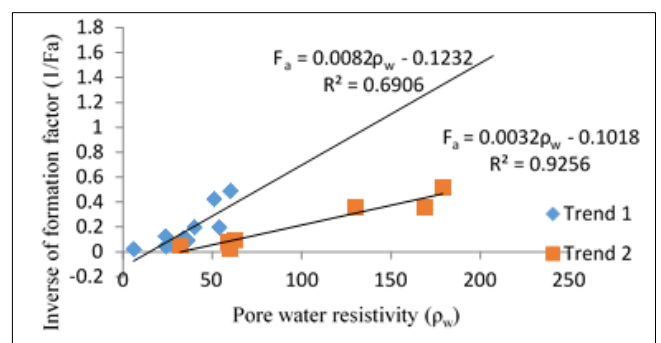
$$\frac{1}{F_a} = 0.0082\rho_w - 0.1232 \tag{9}$$

With a correlation coefficient of,  **$R^2 = 0.70$** .

And Trend 2,

$$\frac{1}{F_a} = 0.0032\rho_w - 0.1018 \tag{10}$$

Having a correlation factor of,  **$R^2 = 0.93$** .



**Fig 6:** Inverse of formation factor ( $1/F_a$ ) plotted against pore water resistivity ( $\rho_w$ )

The extremely high values of Formation factor in some locations indicates the presence of high bulk resistivity (resistive dispersed phase) and very low Pore water resistivity (conductive continuous phase). Since the Formation factor ( $F_a$ ) is dependent on bulk as well as electrolyte resistivity, it is therefore summarily evidenced that Formation factor ( $F$ ) increases with increase in mean grain size, and consequently higher pore water resistivity (Salem, 2001) [1].

The distribution map of the Formation factor of the study area is shown in Fig. 7. Formation factor evaluated ranges between 1.41 and 47.5 with an average of 12.49 (Table 1). The spatial distribution map of formation factor in the study area is shows that formation factor is of highest values in the east central parts of the study area.

Although Formation factor depends on the behaviour of the porous media, we attribute the relatively low Formation factor values, to low pore water resistivity (which ranges from, 6 - 179 Ωm, average 69.2 Ωm), as well as high bulk resistivity values (ranging from, 82 - 1894 Ωm, average 441 Ωm).

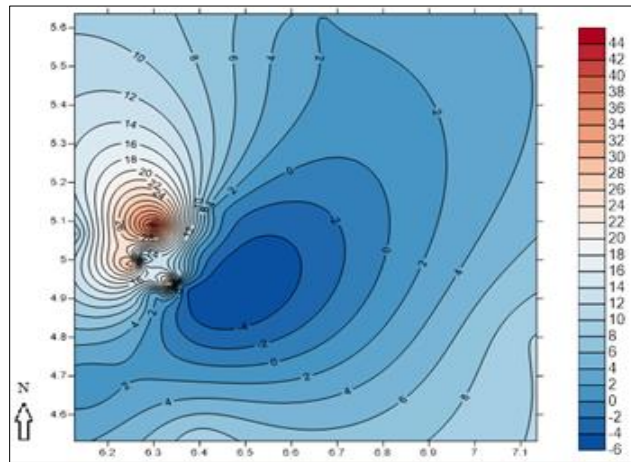


Fig 7: Distribution map of formation factor (Fa) in the study area

**4.2 Porosity**

The estimated porosity in the study area ranges from 12 to 57%, at VES stations of 7, 34 and 21. The spatial distribution of the estimated porosity is shown in Fig. 8. The Porosity values obtained from the inversion of VES modelled parameters (Table 1) show that the porosity (φ) values range from 12% to 57%. The spatial distribution map of the estimated porosity is presented in Fig. 8, the Fig. shows that porosity values vary spatially from low values

around the west central and south western parts to relatively high values around the north eastern parts of the study area. The calculated porosity values of an aquifer using average resistivity values are considered average porosity values, this is worthy of note because the resistivity values obtained from VES analysis are themselves average values, constructed from all of the smaller scaled heterogeneities within each layer (Soronnadi-Ononiwu, 2015)<sup>[13]</sup>.

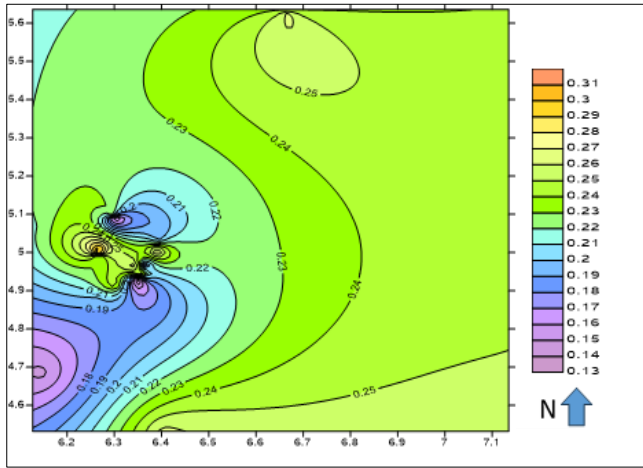
Table 1: Estimated formation resistivity factor and intrinsic formation factor (Fi)

VESL	ρ <sub>w</sub>	ρ <sub>b</sub>	σ <sub>b</sub>	σ <sub>w</sub>	F <sub>a</sub>	1/F <sub>a</sub>	1/F <sub>c</sub>	φ <sub>VES</sub>	φ <sub>VES</sub> (%)
2	59	737.5	0.0014	170	12.50	0.08	0.10	0.25	25
3	43	1893.9	0.0005	168	31.3	0.03	0.10	0.25	25
4	51	120.9	0.0083	197	2.37	0.14	0.24	0.39	39
5	135	1000.0	0.0010	74	7.41	0.14	0.28	0.42	42
6	130	364.8	0.0027	77	2.81	0.36	0.04	0.16	16
7	6	285.0	0.0035	1660	47.50	0.02	0.03	0.12	12
8	54	702.4	0.0014	148	21.9	0.05	0.12	0.27	27
9	169	472.9	0.0021	59	2.80	0.36	0.16	0.32	32
10	40	207.0	0.0048	118	20.9	0.18	0.12	0.27	27
11	24	195.5	0.0051	496	20.0	0.05	0.13	0.28	28
12	179	345.9	0.0029	56	1.93	0.52	0.03	0.14	14
13	60	122.8	0.0081	167	2.05	0.02	0.43	0.52	52
14	36	400.0	0.0025	278	11.11	0.03	0.24	0.39	39
16	54	181.0	0.0055	284	1.26	0.19	0.22	0.37	37
17	24	368.0	0.0027	250	1.41	0.04	0.14	0.29	29
18	38	4135.0	0.0002	260	2.11	0.18	0.11	0.25	25
21	180	645.0	0.0016	160	10.32	0.05	0.50	0.57	57
22	34	103.9	0.0096	2300	17.78	0.09	0.17	0.32	32
26	48	298.0	0.0034	295	8.79	0.11	0.25	0.40	40
33	63	645.0	0.0160	160	1.89	0.1	0.40	0.50	50
34	27	290.0	0.0034	583	16.91	0.06	0.02	0.12	12

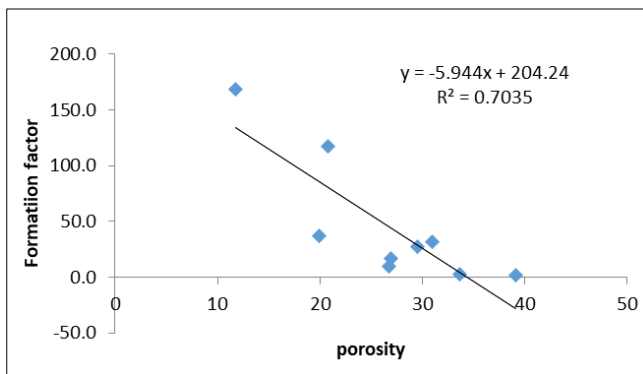
**4.3 Formation factor correlated with Porosity**

Formation factor plotted against porosity (φ) is presented in Fig. 9. Fig. 9 shows that Formation factor is related to porosity (φ) in an inverse fashion. The associated regression equation is expressed as;  
 $F_a = 204 - 5.94\phi$

And has a correlation coefficient (R<sup>2</sup>) of 0.70. (11)



**Fig 8:** Distribution map of VES porosity (fractional)



**Fig 9:** Formation factor against porosity

### Conclusion

Electric formation factor and porosity are vital aquifer hydraulic parameters in the geosciences. The present study has undertaken an estimation of formation factor and porosity from Vertical Electrical sounding survey.

Formation factor (Fa) is dependent on bulk resistivity as well as aquifer electrolyte resistivity, it is therefore summarily evidenced that Formation factor (F) increases with increase in mean grain size, and consequently higher pore water resistivity (Salem, 2001) [16]. The spatial distribution map of formation factor in the study area shows that formation factor is of highest values in the east central parts of the study area. The study further reveals that porosity values vary spatially from low values around the west central and south western parts to relatively high values around the north eastern parts of the study area.

### Acknowledgment

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